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Pythagoreanism in the *Meno*

and

Platonic Development

Πλάτων δὲ καὶ ἐν τούτοις πυθαγορίζει

Diels DG p. 335

This paper will be tripartite in structure. In a short first part I shall indicate what appears to be Aristotle's idea of Platonic development. In the main middle section, Pythagorean factors in the *Meno* will be detected and analyzed. And then the question as to the "meaning" of this dialogue will be addressed in the final part, what main point, namely, if anything, Plato wanted to bring to his readers' awareness by writing and publishing this work. The intimate connection among these three parts will become manifest as they are unfolded.

Ι

In his critical history of philosophy (*Metaphysics* A, and further M and N), Aristotle clearly and unmistakeably (however we may interpret or account for it) considers Plato (just as his immediate successors in the Old Academy) a sort of Pythagorean. By Pythagoreanism in this paper I shall mean basically what Aristotle signified, when he described the proper and peculiar characteristic of that "school" of thought: οί δὲ Πυθαγόρειοι δύο μὲν τὰς ἀρχὰς κατὰ τὸν αὐτὸν εἰρήκασι τρόπον (i.e. one ἐν ὕλης εἴδει, the other τὴν ὅθεν ἡ κίνησις - this being Aristotle's reduction (συνάγειν) of what the previous thinkers expressed μορυχώτερον, to his systematic theory of causality), τοσοῦτον δὲ προσεπέθεσαν δ καὶ ἴδιόν ἐστιν αὐτῶν, ὅτι τὸ πεπερασμένον καὶ τὸ ἄπειρον καὶ τὸ εν οὐχ ἑτέρας τινὰς ψήθησαν εἴναι φύσεις, οἶον πῦρ ἢ γῆν ἡ τι τοιοῦτον ἔτερον, ἀλλ' αὐτὸ τὸ ἄπειρον καὶ αὐτὸ τὸ εν οὐσίαν εἴναι τούτων ὧν κατηγοροῦνται, διὸ καὶ ἀριθμὸν εἴναι τὴν οὐσίαν πάντων (Met. 987a13-19). Aristotle furthermore

associates to this, let us say, "mathematization" of reality, the beginning of the systematic search for definitions of the essential nature of things (καὶ περὶ τοῦ τί ἐστιν ἤρξαντο μὲν λέγειν καὶ όρίζεσθαι, 987a20-21), although their treatment was simplified (λίαν δ' άπλῶς ἐπραγματεύθησαν, ibid.). The simplicity of their definitional procedure consisted, according to Aristotle, first in that their definitions were touching superficially the real essence of things, and secondly, and particularly, in that they took the first term of a series as the essence of the common character of the series (Formulaicly put, the essence of F, or of F-ness, in the F-series F_1 , F_2 , F_3 , ..., F_n , ... is F1): ὡρίζοντό τε γὰρ ἐπιπολαίως, καὶ ῷ πρώτῳ ὑπάρξειεν ὁ λεχθεὶς ὄρος, τοῦτ' εἶναι τὴν οὐσίαν τοῦ πράγματος ἐνόμιζον, ὥσπερ εἴ τις οἴοιτο ταὐτὸν εἶναι διπλάσιον καὶ τὴν δυάδα διότι πρῶτον ὑπάρχει τοῖς δυσὶ τὸ διπλάσιον. ἀλλ' οὐ ταὐτὸν ἴσως ἐστὶ τὸ εἶναι διπλασίω καὶ δυάδι (987a22-26). The bearing of this on the theory of forms, esp. in connection with the difficulty of explaining their relationship to existents in space and time, is evident. As it is its relevance to the Aristotelian notion of πρὸς εν λέγεσθαι, as a means of avoiding such difficulties in some appropriate cases.

By employing here the above Aristotelian understanding of fundamental Pythagoreanism, I accept the implication that this was the relevant and dominant form of Pythagorean Philosophy in the 5th century, although I have argued elsewhere that such a construal is inapplicable to (or, at least, seriously misleading for), 6th century Pythagoreanism (and also explained how the transformation came about).

In his account of the PrePlatonic (and *not* Presocratic) philosophy, Aristotle lays the leading emphasis on the Pythagoreans. The Eleatic singularity is fully acknowledged (986b8 – 987a2): but he highlights the fact that Parmenides, the more penetrating Eleatic (μᾶλλον βλέπων 986b 28), was obliged to postulate himself *dualism* in his theory of the sensible world (ἀναγκαζόμενος δ' ἀκολουθεῖν τοῖς φαινομένοις 986b 31). Aristotle recapitulates the point and significance of Pythagoreanism (987a2-28) just before he turns his analytic attention to what he clearly considers as a new phase in philosophy, Plato (and his Academy).

Μετὰ δὲ τὰς εἰρημένας φιλοσοφίας ἡ Πλάτωνος ἐπεγένετο πραγματεία, τὰ μὲν πολλὰ τούτοις ἀκολουθοῦσα, τὰ δὲ καὶ ίδια παρὰ τὴν τῶν Ιταλικῶν ἔχουσα φιλοσοφίαν (987a29-31). Who the "Italics" are is clear from what follows. Aristotle seems to ascribe implicitly to the Platonic "systematic treatment of things", (πραγματεία is significantly used in this connection to differentiate the Platonic "system" from the preceding philosophical endeavours), a certain eclecticity. Many characteristics of it were taken up, we are told, or were elaborate follow ups, from those previous philosophies, while its peculiar tenets came from the "Italics". These Italics are identified afterwards as Pythagoreans (987b11; b23; b31; and, definitively, 988a26, where the "Italics" are credited with making the ἄπειρον principle of reality). For one reason or another, and probably because he did not thought of it as such a cardinal contribution to the history of philosophy, Aristotle discounts, in this respect, too, the Eleatics.

The peculiar identity ($\tau \dot{\alpha}$ $\check{\iota}\delta\iota\alpha$) of Platonism is, then, according to Aristotle, its Pythagoreanism. Furthermore, Aristotle is crystal clear about the basic structure of that system, as well as of its historical genesis: here again the essence of the system and its origination (growth) reveal the same reality from alternative points of view, one systematical, the other historical; both points of view combine in the concept of $\phi \dot{\nu} \sigma \iota \varsigma$.

The general structure of the Platonic system is described by Aristotle in two fundamental doctrines (with one substantial corollary):

- 1) There are separate ideas of particular things exhibiting a common character ("Theory of Forms"). In terms of the series-model that I used above, there is an F *per se* for every series F_1 , F_2 , ..., F_n , ..., and this F (not F_1) is the essence of all F's. (There are certain qualifications to this general proposition, but they do not affect its fundamental significance).
- 2) The ideas are (ideal) numbers. The principles of numbers are the principles of reality. Pythagorean Dualism provides these two principles, with a Platonic qualification (the second principle is itself dual rather than unitary) and a complication (the "matter" of the sensible things is the same second principle as the substratum for the ideas, 988a11-14; ct. *Physica* 209b11-16).

The significant corollary from (1) and (2) is that the numbers as causes of being cannot for Plato be the mathematical numbers, for these are many of a kind. Thus in between ideas = ideal numbers and material reality, there lie the mathematicals (through which ideas

shape the sensible world by imposing form and order on "matter" = on the second principle of being). The necessity for the existence of these intermediate entities is clear: ἔτι δὲ παρὰ τὰ αἰσθητὰ καὶ τὰ εἴδη τὰ μαθηματικὰ τῶν πραγμάτων εἶναί φησι μεταξύ, διαφέροντα τῶν μὲν αἰσθητῶν τῷ ἀΐδια καὶ ἀκίνητα εἶναι, τῶν δὲ εἰδῶν τῷ τὰ μὲν πόλλ' ἄττα ὅμοια εἶναι τὸ δὲ εἶδος αὐτὸ ε̂ν ἕκαστον μόνον, 987b14-18.

To this structural account of the Platonic system, there exactly corresponds its genetic explanation. This is also basically binary:

- 1*) Heracleitianism + Socratic quest for definition, which means for the common universal (τὸ καθόλου), \Rightarrow theory of forms [987a32-987b1: Heracleitean influence via Cratylus. 987b1-9: Socratic contribution].
- 2*) Pythagoreanism explains the identification of ideas with (ideal) numbers and the theory of first principles (987b18-25).

There is in fact such an explicit nexus of cross-inferences in Aristotle's account of the Platonic system, that his reconstruction appears thoroughly deliberate. Thus, because of (1), and, correspondingly, (1*), numbers and their principles are separate from things, unlike what is the case according to the Pythagorean theory. Τὸ μὲν οὖν τὸ ε̂ν καὶ τοὺς ἀριθμοὺς παρὰ τὰ πράγματα ποιῆσαι (sc. Plato), καὶ μὴ ἄσπερ οἱ Πυθαγόρειοι, καὶ ἡ τῶν εἰδῶν εἰσαγωγὴ διὰ τὴν ἐν τοῖς λόγοις ἐγένετο σκέψιν (οἱ γὰρ πρότεροι διαλεκτικῆς οὺ μετεῖχον), 987b29-33. And, conversely, we may add, because of (2), and (2*), the essence of things and their sensible cosntitution, have ultimately to be interpreted mathematically, as in *Timaeus*. Finally, (1*) and (2*) lead to:

3*) The conjuction, and synthesis, of Heracleiticism + Socratism on the one hand and Pythagoreanism on the other leads to the Platonic peculiarity of *mathematical intemmediacy*, a doctrine which introduces into the system heavy additional complications according to Aristotle, and which, significantly was abandoned by Speusippus (οἱ λέγοντες ἀριθμὸν πρῶτον τὸν μαθηματικόν, 1075b37). The Old Academy reverted then to purer Pythagoreanism after Plato.

Now the crucial (for our purpose here) question in Aristotle's account of the Platonic system is whether he understood (1*) and (2*) as two distinct temporal *phases* in the formation of the system, or rather as two steps in the logical *construction* of the system, two "steps" reflecting the two moments (1) and (2). And the answer to this question depends heavily on Aristotle's meaning in the passage where he critically re-examines the Theory of Forms in M, 4-5. He starts this inquiry in the following way: $\pi \epsilon \varrho i$ δὲ τῶν ἰδεῶν $\pi \varrho$ ῶτον αὐτὴν τὴν κατὰ τὴν ἰδέαν δόξαν ἐπισκεπτέον, μηθὲν συνάπτοντας $\pi \varrho$ ὸς τὴν τῶν ἀριθμῶν φύσιν, ἀλλ' ὡς ὑπέλαβον ἐξ ἀρχῆς οἱ πρῶτοι τὰς ἰδέας φήσαντες εἶναι (1078b9-12). Who are these $\pi \varrho$ ῶτοι τὰς ἰδέας φήσαντες εἶναι μηθὲν συνάπτοντες $\pi \varrho$ ὸς τὴν τῶν ἀριθμῶν φύσιν? I think Plato (and not, e.g., some other Socratic φίλοι τῶν εἰδῶν).

In support of this thesis I shall simply mention here that the argumentation in M parallels closely the corresponding one in A, where Plato is obviously the object of inquiry. In particular, the role of the Socratic quest for definition of the essential $\kappa\alpha\theta\delta\lambda$ ov is highlighted, again in the context of dominant Heracleitianism.

Socrates is here, moreover, explicitly denied the patronage of the Theory of Forms: $\dot{\alpha}\lambda\lambda'$ ό μὲν Σωκράτης τὰ καθόλου οὐ χωριστὰ ἐποίει οὐδὲ τοὺς ὁρισμούς· οἱ δ' ἐχώρισαν, καὶ τὰ τοιαῦτα τῶν ὄντων ἰδέας προσηγόρευσαν (1078b30-32). In fact, Socrates is equally explicitly credited with two things (δύο γάρ ἐστιν ἄ τις ἄν ἀποδώη Σωκράτει δικαίως, 1078b27-8), τοὺς τ' ἐπακτικοὺς λόγους καὶ τὸ ὁρίζεσθαι καθόλου (1078b28-29), both pertaining to scientific knowledge (ταῦτα γάρ ἐστιν ἄμφω περὶ ἀρχὴν ἐπιστήμης, 1078b29). And Socrates' interest was restricted even in this respect to the *moral excellences* (virtues), περὶ τὰς ἡθικὰς ἀρετὰς πραγματευομένου (1078b17-18); cf. 987b1-2: Σωκράτους δὲ περὶ μὲν τὰ ἡθικὰ πραγματευομένου περὶ δὲ τῆς ὅλης φύσεως οὐθέν etc.

That Plato is primarily meant in this criticism of the Theory of Ideas in M, 4-5, is further evidenced by the fact that near the end of the entire argumentation the *Phaedo* is mentioned by name (1080a2). And this again replicates what is said about the same Phaedonian point in A, 991b3 sqq.

Finally, on a different count, that Plato actually underwent a fundamental evolution in thinking according to Aristotle, seems also to be suggested by the way in which he temporalises his account of the constitutive influences on Plato's formation, in the very introduction of his examination of Platonic philosophy. Thus Plato ἐκ νέου τε γὰο συνήθης γενόμενος πρῶτον Κοατύλφ καὶ ταῖς Ἡρακλειτείοις δόξαις (987b32-33), inferred that there can be no science of the sensible reality as this is found in continuous flux. Ταῦτα μὲν καὶ ὕστερον οὕτως ὑπέλαβεν (987a34-b1): i.e. he retained

this Heracleitean influence in the latter and maturer phases of his thinking. Then comes the Socratic factor, and finally Pythagoreanism is introduced. The sequence is of course repeated in the latter treatment (M, 4-5).

In conclusion, therefore, Aristotle provides us with an analytical and genetic description of the fundamental structure of the Platonic system, which admits of a two-stage pattern in Platonic development: the stage before and the stage after some decisive exercise of Pythagorean influence. The stage before is dominated by Heracleiteanism (sensible reality is in permanent flux) and Socratism (definition and science is of the universal). These parameters continued to operate into the second phase of Pythagorean under the overarching Platonism, but now influence Pythagoreanism, which in effect gave the key to the knowledge logically demanded, but not discoverable, within the framework of the first phase. But more on this, in the third section below.

Let me mention here (what will be elaborated in an Appendix) that Aristotle's account of Platonic development, also squares nicely with the historical evidence, as this can be elicited from the critical shifting of our sources.

II

Pythagoreanism in the *Meno* will be analysed here under the following seven headings:

1) Socrates' example of a proper definition: shape, colour and their intimate connection (74b4-76e9).

- 2) The doctrine of reincarnation (specifically in its Pindaric form). Who are the ἄνδρες καὶ γυναῖκες σοφοὶ περὶ τὰ θεῖα πράγματα? (81a5-c4).
- 3) Άνάμνησις (81c5 sqq.).
- 4) The kinship of nature and the cohesion of knowledge (81c9-d4).
- 5) The mathematical demonstration with the slave and inferences from it concerning ἀνάμνησις (82b9-86c2). The meaning of ἀεὶ ἡ ἀλήθεια τῶν ὄντων ἐστὶν ἐν τῆ ψυχῆ (86b1-2).
- 6) Argumentum ex hypothesi (86d3-87c2).
- 7) Λογισμὸς αἰτίας (98a3-4).
- 1) Wanting to give an example of what he means by a proper definition of the essence of a thing, Socrates proposes shape as object of investigation (τί ἐστιν σχῆμα; 74b5). A mathematical entity is thus focused upon. And in immediate succession to the question, colour (χρ $\tilde{\omega}$ μ α) is introduced (74c5). Then without much ado (apart from generalities that do not relate directly to the particular case under discussion), the following statement is given as an answer to the τ i ἐστιν question: ἔστω γὰο δὴ ἡμῖν τοῦτο σχῆμα, δ μόνον τῶν ὄντων τυγχάνει χοώματι ἀεὶ ἑπόμενον (75b9-11). Now that the existence of colour entails the existence of a (coloured) surface is an important point that could be developed philosophically in important ways. One should expect here pregnant explanatory analyses on the relationship of surface, boundary of a solid thing and colouration. Nothing, however, of the sort is being attempted here. The development is blocked by Meno's objection that this is to define unknowns by things more unknown (75c2-7). On the other hand, it

was a characteristic Pythagorean tenet to essentially associate surface with colour; in fact, Aristotle seems to indicate that the Pythagoreans identified surface and colour: τὸ γὰο χοῶμα ἢ ἐν τῷ πέρατί ἐστιν ἢ πέρας (διὸ καὶ οἱ Πυθαγόρειοι τὴν ἐπιφάνειαν χρόαν ἐκάλουν), Parva Naturalia, 439a30-31 = 58DK B42. (Doxographic attestation in -Plut. Epit. I, 15, 2 = Stobaeus Ecl. I, 16, 2 = Diels DG p. 313.6-7: of Πυθαγόρειοι χροιάν ἐκάλουν τὴν ἐπιφάνειαν τοῦ σώματος, where it is made explicit that a surface is the boundary of a body. And so Psellus, de omnit. Doctr. 64: χρῶμά ἐστιν ὁρατὴ ποιότης τῆς τῶν σωμάτων ἐπιφανείας, where the force of the Pythagorean conception is rather scholastically lost or diluted). In the Theolog. Arithm. the doctrine (p. 22.5 de Falco) appears in conjunction with the Pythagorean emphasis on the surface as fundamental element in the geometry of space (and, thus, in the constitution of solids mathematical or physical is the same thing for the Pythagoreans). As Aristotle mentioned with reference to some thinkers (including the Pythagoreans), boundaries and limits of bodies are substances, and more so than bodies and solids (Met. 1028b16 = 58 DK B23). – $X_{Q} \dot{o} \alpha$, χροιά (and χρώς) meant also the skin esp. of the human body and its complexion, as well as colour. The essential association of bounding surface and colour was felt even in the prephilosophical understanding of the world reflected in language and common thinking.

Furthermore. We know something about how, according to the Pythagoreans, colour entered into the very first cosmogonical step. Aristotle comments on what he deems a difficulty on their part to account for the generation of the first one from the ultimate dual principles of reality, πέρας καὶ ἄπειρον. This first one is an extended unit by means of which space (in itself an infinity) is organized into finite order. But ὅπως δὲ τὸ πρῶτον εν συνέστη ἔχον μέγεθος, ἀπορεῖν ἐοίκασιν (Met. 1080b20-21 = 58 DK B9). An intimation of the different approaches which the Pythagoreans utilised to overcome this difficulty in effecting the first step towards the world creation, is given by Aristotle: φανερῶς γὰρ λέγουσιν ὡς τοῦ ένὸς συσταθέντος, εἴτ' ἐξ ἐπιπέδων εἴτ' ἐκ χροιᾶς εἴτ' ἐκ σπέρματος εἴτ' ἐξ ὧν ἀποροῦσιν εἰπεῖν, εὐθὺς τὸ ἔγγιστα τοῦ ἀπείρου ὅτι εἵλκετο καὶ ἐπεραίνετο ὑπὸ τοῦ πέρατος (Met. 1091a 15-18 = 58DK B26). Cf. Philolaus (44DK B7): τὸ πρᾶτον άρμοσθέν, τὸ ἕν, ἐν τῷ μέσῳ τᾶς σφαίρας ἑστία καλεῖται. And so Theolog. Arithmeticae p. 6.17 (de Falco): τὴν μοναδικὴν φύσιν Έστίας τρόπον ἐν μέσω ίδοῦσθαι. More informatively, Philolaus 44DK Β17: ὁ κόσμος εἶς ἐστιν, ἤοξατο δὲ γίγνεσθαι ἀπὸ τοῦ μέσου καὶ ἀπὸ τοῦ μέσου εἰς τὸ ἄνω διὰ τὼν αὐτῶν τοῖς κάτω.

[[The passage continues: ἔστι <γὰο> τὰ ἄνω τοῦ μέσου ὑπεναντίως κείμενα τοῖς κάτω. τοῖς γὰο κατωτάτω τὰ μέσα ἐστὶν ὥσπεο τὰ ἀνωτάτω καὶ τὰ ἄλλα ὡσαύτως. πρὸς γὰο τὸ μέσον κατὰ ταὐτά ἐστιν ἑκάτεοα, ὅσα μὴ μετενήνεκται. This idea is explicitly mentioned (without organic need) in Socrates' description of the underworld (inside the "real earth" which is vastly larger than what we think "our earth" and extends to the heaven, is, in fact, the entire world) in Phaedo's myth (112d6-e3). Philolaus held that the moon was γεώδης and inhabited καθάπεο τὴν παρ' ἡμῖν γῆν (44DK A20). He also called Ὁλυμπον τὸ ἀνωτάτω μέρος τοῦ περιέχοντος, ἐν ῷ τὴν

εἰλικοίνειαν εἶναι τῶν στοιχείων (44 DK A16) – of all elements presumable and, of earth above all, just as in the Phaedonian myth (109b4-c2; 109d6-110b2; cf. 110b sqq.; 114b6-c2). This extremely characteristic conception of a World-Earth is ascribed by Plato to someone specifically: εἰσὶν δὲ πολλοὶ καὶ θαυμαστοὶ τῆς γῆς τόποι, καὶ αὐτὴ οὕτε οἵα οὕτε ὅση δοξάζεται ὑπὸ τῶν περὶ γῆς εἰωθότων λέγειν, ώς ἐγὼ ὑπό τινος πέπεισμαι (Phaedo, 108c5-8). This "one" must have been then Philolaus, who is also mentioned explicitly in the dialogue (61e), in connection with the prohibition of self-slaying resulting from the doctrine of the soul's incarceration in the bodily life of this world (cf. 44DK A15 and A14).

[The idea of World-Earth, with its multitude of deeper or shallower, broader or narrower, interconnected cavities (ἔγκοιλα, Phaedo 111c5), one of which is our οἰκουμένη, this idea goes back in all likelihood to Phyrecydes (v. 7DK B6; cf. A10). The Philolaean lengthy and elaborate recension of the idea (ὁ βίος μοι δοκεῖ ὁ ἐμός, ἄ Σιμμία, τῷ μήκει τοῦ λόγου οὐκ ἐξαφκεῖν, Phaedo 108d8-9) must have been impressive and influential. Clearchus (the Peripatetic) seems to have used it in recounting the death-experience (Er-like) of Cleonymus (Fr. 8, p. 11.35 sqq. Wehrli): τὴν μὲν οὖν αὐτοῦ ψυχὴν φάναι παρὰ τὸν θάνατον οἶον ἐκ δεσμῶν δόξαι τινῶν ἀφειμένην τοῦ σώματος παρεθέντος μετέωρον ἀρθῆναι, καὶ ἀρθεῖσαν ὑπὲρ γῆς ἰδεῖν τόπους ἐν αὐτῆ παντοδαποὺς καὶ τοῖς σχήμασι καὶ τοῖς χρώμασιν καὶ ρεύματα ποταμῶν ἀπρόσοπτα ἀνθρώποις. καὶ τέλος ἀφικέσθαι εἴς τινα χῶρον ίερὸν τῆς Εστίας etc., where the souls undergo punishment

and purification (as in the Acherusian lake of the Phaedonian myth)].

It is significant that the Phaedonian myth lays extraordinary stress on the colouration of the real earth and its parts, as it is seen from the purity of the celestial sphere: 110b7-e2. The emphasis on colour as a fundamental cosmogonical factor may have been characteristic of Philolaus. It was remarkably reflected in Zeno the Stoic: Ζήνων ὁ Στωϊκὸς τὰ χοώματα πρώτους εἶναι σχηματισμοὺς τῆς ὅλης *Plut. Epit.* I, 15, 6 = Stobaeus I, 16.6 = Diels DG p. 313.19-20).]]

Aristotle, we saw, mentions planes, colour-surfaces and semen as ways which different groups of Pythagoreans endeavoured to invoke in order to explain the beginning of the world-ordering, the genesis of the first extended monad out of the two principles of reality. I have argued elsewhere [Origin and Nature of Early Pythagorean Cosmogony, in K. Boudouris (ed.), Pythagorean Philosophy, 1992, pp. 126-162, esp. pp. 135 sq. with notes] in favour of an original form of Pythagoreanism that would employ biological symbolism (semen) in its cosmogonical processes. Planes, on the other hand and at the other end, seem to refer to a construction of (regular geometrical) solids out of plane figures, like the elementary triangles in Plato's Timaeus. Colour-surfaces (in between the two extremes conceptually and chronologically), may well reflect the idea that it is the boundaries of bodies which constitute them as distinct entities, with unorganized space or the vacuum separating them one from another: εἶναι δ' ἔφασαν καὶ οἱ Πυθαγόρειοι κενόν, καὶ ἐπεισιέναι αὐτῷ τῷ οὐρανῷ ἐκ τοῦ ἀπείρου πνεῦμα τε ὡς ἀναπνέοντι καὶ τὸ κενόν, δ διορίζει τὰς φύσεις, ὡς ὄντος τοῦ κενοῦ χωρισμοῦ τινος τῶν ἐφεξῆς καὶ [τῆς] διορίσεως καὶ τοῦτ' εἶναι πρῶτον ἐν τοῖς ἀριθμοῖς τὸ γὰρ κενὸν διορίζειν τὴν φύσιν αὐτῶν (numbers being extended entities for the Pythagoreans), *Phys.* 213b22 = 58 DK B30.

According to such a construal, it is boundaries of things that we perceive as shapes and as colours. These colour-surfaces even have a certain metaphysical priority over their bodies: they define them as existing, distinct and separate entities. This account would fit well to the Orphic doctrine of Protogonos-Eros' birth (with its portentous light-imagery that accompanies him right from the beginning, as in Aristophanes' Aves). Light (of Phanes, according to Orphism) brings to existential "appearance" the multifarious hues which constitute the variegated spectacle of reality. This could also explain the apparent definitional precedence of colour over surface in both the Pythagorean and the Menonian accounts: οἱ Πυθαγόρειοι την ἐπιφάνειαν χρόαν ἐκάλουν. And: σχημά ἐστιν ο μόνον τῶν ὄντων τυγχάνει χοώματι ἀεὶ ἑπόμενον. (This would come from a phase of Pythagoreanism preceding the fully mathematicised one, with its stress on surfaces, Timaeus-like, in the constitution of sensible reality).

[Such an Orphic connection would square with the cosmogonical content of (the reputed Philolaus') Bάκχαι (44DK B17-19). We should always bear seriously in mind the Herodotean pronouncement (even if it is given with reference to a particular observance): ὁμολογέουσι δὲ ταῦτα τοῖσι Ὀρφικοῖσι καλεομένοισι καὶ Βακχικοῖσι, ἐοῦ δὲ Αἰγυπτίοισι καὶ Πυθαγορείοισι (II 81). Maybe the

Phaedonian myth comes from the Philolaean system of cosmology and eschatology].

After the repudiation by Meno of the proposed definition, Socrates agrees that in a dialectical encounter perhaps one should state only what the person questioned admits of knowing. There follows then the geometrical definition of shape: στεφεοῦ πέφας σχῆμα εἶναι (76a7). Meno presses on for a definition of colour. Socrates obliges with the Gorgean (basically Empedoclean*) account: ἔστιν γὰφ χφόα ἀποφφοὴ σχημάτων ὄψει σύμμετφος καὶ αἰσθητός (76d4-5). If σχημάτων is right, we probably have a Platonic elaboration of Empedocles – Gorgias view. Χφημάτων is attested as a variant in T, while σωμάτων is read in Alexander *de sensu* p. 24.8 (Wendland). If the definition is Gorgias', χφημάτων should be probably restituted, as Diels-Kraunz saw. Πόφοι played an important generally role, it seems, in Gorgian Physics, cf. 82 DK B5.

Socrates makes clear that he is not satisfied with this definition of colour (76e6-9). He ascribes Menon's enthousiastic endorsement of it to the fact that he is accustomed to it (76d8) or that it is framed grandiloquently (e3-4) in Gorgian rhetorical manner. Socrates means probably to object that it does not give the essence of colour, but only, *at most*, supplies an account of the mechanism through which colour is seen. (This is exactly what he clarifies in the methodological

Theophrastus (*de sensibus*_§7 = Diels DG p. 500.19 sqq.) ascribes the view to Empedocles. Aristotle ascribes to him variation of opinion (*de sensu*, 437b23 – 438a5: Ἐμπεδοκλῆς δ' ἔοικε νομίζοντι ότὲ μὲν ἐξιόντος τοῦ φωτός, ὥσπερ εἴρηται πρότερον, βλέπειν ... ότὲ μὲν οὖν οὕτως ὁρᾶν φησίν, ότὲ δὲ ταῖς ἀπορροίαις assigns ταῖς ἀπὸ τῶν ὁρωμένων).

passage of *Phaedo*). Besides, the Pythagorean factor operating here would demand definitions of shape and colour exhibiting the necessary coimplication, if not virtual identity, of their respective objective essences.

2) The doctrine of transmigration and reincarnation of the souls was peculiarly Pythagorean. Furthermore, here we have to do with a specific form of it encapsulated in the Pindaric passage (Fr. 133 Maehler). According to this, the incarnated souls are giving penance for wrongs done of old, for ancient mourning and "pristine woe" (ποινὰν παλαιοῦ πένθεος). The primeval grief is Persephone's (as Rhode saw) primarily – her is the $\pi \dot{\epsilon} \nu \theta o \varsigma$, and therefore she is entitled to receive, accept or refuse, atonement. In the Pindaric text we meet therefore by implication with the abominable deeds of the Titans committed upon Zagreus, the Mysteric Dionysus, son of Persephone. The full Orphic account of the story of this Original Sin had the Titans struck by Zeus' lightning. From their ashes came the human race, Τιτανικὸν σπέρμα. In the Pindaric fragment we see also part of the Orphic-Pythagorean eschatology. It concerns those that are relieved from the bondage of necessity: κύκλου δ' ἐξέπταν βαουπενθέος ἀργαλέοιο, as the gold leafs of the dead had it. They are the εὐσεβεῖς and ὄλβιοι of Fr. 129. (The Orphic tenor of the doctrine is confirmed by Fr. 131a: ὄλβιοι δ' ἄπαντες αἴσα λυσιπόνων τελετᾶν). In Fr. 130 we encounter the damned souls, the ones condemned to the Tartarean Erebus. There remains the third part of souls, of the middling life on earth, who, chastised for their defects for a set period of time, are thrown back to the cycle of innerworldly necessity to prove whether the chastisement was really atonement and purgation. This triple destiny is paralleled in *Olymp*. II 56-78.

Now the structure of this Pindaric (Orphico-Pythagorean) Eschatology is identical with that of the Phaedonian myth. And, so far as we can judge, the cosmology that goes with such Eschatology is also very similar. (See, e.g., the $\pi o \tau \alpha \mu o i$ in Fr. 130). We saw reason above to suport a Philolaean source for Phaedo's myth. But the Pindaric eschatology, (which is by no fortuitous accident that Plato invokes in the *Meno*) leads us way back, to 6th century Orphico-Pythagorean doctrine.

It cannot be without significance that relatively minor, but charateristic, details appear in common among these various cosmologico-eschatological accounts, strengthening thereby the case for a single, definite source, esp. as they form an interlapping net like "family resemblances". In the second Ολυμπιονίκης (addressed appositely to a Sicelian victor), Pindar holds that to those souls is salvation delivered who would live a life of purity *three* consecutive times on earth and three in the realm of ded: *Ol.* II 68: ὄσοι δ' ἐτόλμασιν ἐς τοὶς ἑκατέρωθι μείναντες ἀπὸ πάμπαν ἀδίκων ἔχειν ψυχάν etc. Now *thrice* must they choose to live the pure life those that will be transferred to the Islands of the Blessed, beyond the hold of the Cycle of Necessity, in the cognate to the Phaedonian _Pha*drus_myh*, 249a: ἐὰν ἕωνται τοὶς ἐφεξῆς τὸν βίον τοῦτον etc.

The Orphic version emphasised the specific primeval atrocity perpetrated. We can well imagine that the philosophical

Pythagoreans would generalize the delict involved to any violation of cosmic order committed when the soul lives its independent, purely spiritual, life. In Empedocles we have probably both an allusion to the Titanic abominations (31 DK B124:

ὢ πόποι, ὢ δειλὸν θνητῶν γένος, ὢ δυσάνολβον τοίων ἔκ τ' ἐρίδων ἔκ τε στοναχῶν ἐγένεσθε)

and to the general principle (B115). Once fallen, the souls enter the cycle of transmigration (cf. B127), where they should lead a life of purification (νηστεῦσαι κακότητος, B 144) and wisdom (B 132) in order, at the end of an ascending ladder of transformation, that they might finally become what they were before the fall (B146). The same pattern, more philosophically expressed, we see in *Phaedrus* 248a-249d, esp. 248c-d. Very appropriately DK append to Empedocles the *Phaedrus* passage as C. Anklang. [Notice that if the τρὶς μύριαι ὧραι of Empedocles B 115.6 refer to seasons, and if we accept the early reckoning of three seasons in the year, the grand period of transmigration is the same in Empedocles and Plato (*Phaedrus*: 248e9, ἐτῶν μυρίων)].

But whatever the possibilities open, and whatever the significance of an outlook which would emphasise that imprisonment protects (as well as punishes) the culprit from his worst predictable excesses (on which more in a moment), the corporeal "dressing" of the soul, to which she is bound, is a serious "testaceous" impediment to its diine function: initially souls were by themselves following the litany of Zeus and the other gods, $\kappa\alpha\theta\alpha\rho\rho\dot{\rho}$

ὄντες καὶ ἀσήμαντοι τούτου ὁ νῦν σῶμα περιφέροντες ὀνομάζομεν, ὀστρέου τρόπον δεδεσμευμένοι (Phaedrus, 250c).

Incarnated souls are here for a punishment. This World is part of the purification procedure, as much as Hades. In fact, according to the Phaedonian myth, our inhabited earth is just one of the cavities of the world-earth, others (more awsome) being the Acherusian lake and Tartarus itself, all bound in a network of communications. The ideas could within such an outlook naturally arise of the soul, first, really dying when being incarnated (being removed from the fullness of its true and divine life); and, second, of the soul being incarcerated in the body of its worldly existence. The former idea we discover, I think, in Empedocles (B 125):

ἐκ μὲν γὰο ζωῶν ἐτίθει νεκοὰ εἴδε' ἀμείβων (which fragment follows immediately upon B118:

κλαῦσά τε καὶ κώκυσα ἰδὼν ἀσυνηθέα χῶρον).

Both ideas are connected especially with Philolaus, who also draw the corollary that, as a consequence of that state of affairs, self-dying is a wrong which aggravates the condition of the soul. And this corollary is explicitly ascribed to Philolaus in *Phaedo*, 61d7; e7. The secret reason given is that we are here somehow incarcerated: ὁ ἐν ἀπορρήτοις λεγόμενος περὶ αὐτῶν λόγος, ὡς ἔν τινι φρουρῷ ἐσμὲν οἱ ἄνθρωποι (62b2-6). V. 44 DK B15. These views were ascribed by Clearchus to some *Pythagorean* Euxitheus (Fr. 38 Wehrli): ἔλεγεν ἐνδεδέσθαι τῷ σώματι καὶ τῷ τῆδε βίῳ τὰς ἀπάντων ψυχὰς τιμωρίας χάριν, καὶ διείπασθαι τὸν θεὸν ὡς εἰ μὴ μενοῦσιν ἐπὶ τούτοις, ἕως ἄν ἑκὼν αὐτοὺς λύση, πλείοσι καὶ μείζονι ἐμπεσοῦνται τότε λύμαις etc.

Cicero goes back to Pythagoras himself (de senect. 20): vetat Pythagoras injussu imperatoris, id est Dei, de praesidio et vitae statione discendere. (But on $\phi o \theta o \alpha$ as praesidium see in a moment). Philolaus meant probably to ascribe the doctrine to Orpheus when he wrote (B14): μαρτυρέονται δὲ καὶ οἱ παλαιοὶ θεολόγοι τε καὶ μάντιες, ώς διά τινας τιμωρίας ά ψυχὰ τῷ σώματι συνέζευκται καὶ καθάπες ἐν σάματι τούτω τέθαπται. Plato in Gorgias assigns the $\sigma \tilde{\omega} \mu \alpha$ - $\sigma \tilde{\eta} \mu \alpha$ theory to some unspecified wise men: ἤκουσα τῶν σοφῶν ὡς νῦν ἡμεῖς τέθναμεν καὶ τὸ μὲν σῶμά ἐστιν ἡμῖν σημα (493a2-3). What follows has significant implications regarding the true upholder of these views: τῆς δὲ ψυχῆς τοῦτο ἐν ῷ ἐπιθυμίαι εἰσὶ τυγχάνει ὂν οἶον ἀναπείθεσθαι καὶ μεταπίπτειν ἄνω κάτω, καὶ τοῦτο ἄρα τις μυθολογῶν κομψὸς ἀνήρ, ἴσως Σικελός τις ἢ Ἰταλικός, παράγων τῷ ὀνόματι διὰ τὸ πιθανόν τε καὶ πειστικὸν ἀνόμασε πίθον, τοὺς δὲ ἀνοήτους ἀμυήτους, τῶν δ' ἀνοήτων τοῦτο τῆς ψυχῆς οὖ αἱ ἐπιθυμίαι εἰσί, τὸ ἀκόλαστον αὐτοῦ καὶ οὐ στεγανόν, ὡς τετρημένος εἴη πίθος, διὰ τὴν ἀπληστίαν ἀπεικάσας. Τοὐναντίον δὴ οὖτος σοί, ὧ Καλλίκλεις, ἐνδείκνυται ὡς τῶν ἐν Ἅδου -:τὸ ἀϊδὲς δὴ λέγων -οὖτοι άθλιώτατοι ἂν εἶεν, οἱ ἀμύητοι, καὶ φοροῖεν εἰς τὸν τετρημένον πίθον ύδως έτέρω τοιούτω τετρημένω κοσκίνω. Τὸ δὲ κόσκινον ἄρα λέγει, ώς ἔφη ὁ πρὸς ἐμὲ λέγων, τὴν ψυχὴν εἶναι τὴν δὲ ψυχὴν κοσκίνω ἀπήκασεν τὴν τῶν ἀνοήτων ὡς τετρημένην, ἄτε οὐ δυναμένην στέγειν δι' ἀπιστίαν τε καὶ λήθην (493a3-c3). If we substract from this passage the implication of some elaborate theory of the division of soul in distinct parts or faculties (ἐπιθυμητικοί etc.), what remains ought to be ascribed to some one "Westerner", a definite one, who is explained metaphorically (allegorizing) by Plato's immediate

informant. (He, the author of these views, says, ώς ἔφη ὁ πρὸς ἐμὲ λέγων. Cf. also the οὖτος in b3 etc.). Furthermore, in the formula κομψὸς ἀνήρ, ἴσως Σικελός τις ἢ Ἰταλικός, the Σικελὸς κομψὸς ἀνήρ is proverbial, as forming a verse in a poem of Timochares the Rhodian (Fr. 4 Diehl). Hence, Plato means in all probability someone from Magna Graecia (Ἰταλικός). Now it was part of the Orphic symbolic imagery to picture the damned souls as exerting themselves in something miserably self-defeating. Carrying water in a sieve is exemplary in this respect. So Musaeus and Orpheus (according to Plato, Rep. 363c-e) τοὺς ἀνοσίους εὖ καὶ ἀδίκους εἰς πηλόν τινα κατορύττουσιν εν Άϊδου καὶ κοσκίνω ύδωρ ἀναγκάζουσι φέρειν ἔτι τε ζῶντας εἰς κακὰς δόξας ἄγοντες. Differing pictures could have been used to convey the same meaning: Polygnotus painted in the Delphic Λέσχη two women φέρουσαι ὕδωρ ἐν κατεαγόσιν ὀστράκοις, over which he wrote an inscription to the effect εἶναι σφᾶς τῶν οὐ μεμυημένων (Paus. X, 31). To aggravate the force of the initial similitude by making the unjust and unholy ones carry water in a sieve to a perforated jar (τετρημένος π ίθος) is natural to the multidynamism of symbolic thinking. This picture may well have occurred in Philolaus' description of the Earth-World and its eschatological dimensions, not improbably in his *Βακχικά* (where they his in fact). And Philolaus is presumably meant in the Gorgias just before this passage on $\pi i\theta o \varsigma$ and $\kappa o \sigma \kappa i \nu o \nu$ and $\alpha \mu \nu i \eta \tau o i =$ ανόητοι – where Plato mentions the σωμα - σημα theory.

To the negative emphasis on incarnation as incarceration according to the $\sigma \tilde{\omega} \mu \alpha$ - $\sigma \tilde{\eta} \mu \alpha$ theory, there corresponded

complementarily the more positive outlook involved in the $\sigma\tilde{\omega}\mu\alpha$ σώζω account. The body, like prison, protects the culprit from exhausting his depravity and thus aggravating his condition beyond remedy, if he is left unprotected and unbound to himself. The daemonic nature running, so to speak, amok, needs the restrictive bounds of corporeal existence to limit its (self-)wrongdoing. This more constructive attitude to incarnation does not alter the basic metaphysical and eschatological structures of the general theory, as is evident from Plato's testimony: δοκοῦσι μέντοι μοι μάλιστα θέσθαι οί ἀμφὶ Ὀρφέα τοῦτο τὸ ὄνομα (sc. σῶμα) ώς δίκην διδούσης τῆς ψυχῆς, δεσμωτηρίου εἰκόνα. εἶναι οὖν τῆς ψυχῆς τοῦτο, ὤσπερ αὐτὸ ονομάζεται, εως αν εκτείση τὰ οφειλόμενα, σῶμα, καὶ οὐδὲν δεῖν παράγειν οὐδὲ εν γράμμα (Cratylus, 400b-c). The reference is to Zagreus' passion, the Titanic descent of man, atonement for old abominations and all. That Plato here ascribes this aspect of the common basic theory to Orphism, while differentiating it from the more regular one (καὶ γὰο σῆμα τινές φασιν αὐτὸ εἶναι (sc. τὸ σῶμα) τῆς ψυχῆς, ώς τεθαμμένης ἐν τῷ νῦν παρόντι), may indicate a fundamental bifurcation of life-attitudes: a sterner, cathartic, ascetic Pythagorean one contrasted to a more life-accepting, mysteric-therapeutic (perhaps popular) Orphic one, the latter in the spirit of what Plato condemns in Rep. 364e (= 1DK B5). Such a spirit had also respectable philosophical exponents: see eps. Olympiodorus in Phaed. Β, β; Β, ι; B, ιβ; and A, 3 (pp. 2.30-3.5 Norvin). But Plato, his source (Philolaus) and mainstream, orthodox doctrine, conceived of $\phi o \phi o \phi \alpha$ as a place

of chastisement even if for the prisoner's benefit as well. *Gorgias*, 525a6-b4: ἰδὼν (sc. Rhadamanthes) δὲ ἀτίμως ταύτην (sc. the vicious soul) ἀπέπεμψεν εὐθὺ τῆς φρουρᾶς, οἶ μέλλει ἐλθοῦσα ἀντλῆναι τὰ προσήκοντα πάθη. προσήκει δὲ παντὶ τῷ ἐν τιμωρίᾳ ὄντι, ὑπ' ἄλλου ὀρθῶς τιμωρουμένω, ἢ βελτίοι γίγνεσθαι καὶ ὀνίνασθαι ἢ παραδείγματι τοῖς ἄλλοις γίγνεσθαι, ἵνα ἄλλοι ὁρῶντες πάσχοντα ἃ ἂν πάσχη φοβούμενοι βελτίοις γίγνωνται.

To conclude then this part of the inquiry. Who are the ἄνδρες καὶ γυναῖκες σοφοὶ πεοὶ τὰ θεία πράγματα in Meno, 81a? Socrates explains that they are τῶν ἱερέων τε καὶ τῶν ἱερειῶν ὅσοις μεμέληκε περὶ ὧν μεταχειρίζονται λόγον οἵοις τ΄ εἶναι διδόναι (ibid.). Σοφοὶ thus concerning divine things are those who are able to explain them, to reason about them. They make an advance upon the μεμιγμένοι theologians of Aristotle (Met. 1091b8-9), who merely do not employ the pure mythological way alone (such as Pherecydes). Given an Orphic-Pythagorean framework, these sacred persons who are able to reason concerning the mythoritualistic apparatus of religion (and we may well assume, particularly the mytho-logical symbolism of its mysteric aspect), must be Pythagoreans. The emphasis (twice) on men and women points in the same direction. Τερεῖς and ἱέρειαι need not be taken strictly in the connotations of modern priests and priestesses. The rites of ancient religion were open to private citizens, public administrators functionaries of religious or other associations, prophets and soothsayers, holy men, itinerant, even vagabond, initiators and so on.

On the other hand, the doulbe occurrence of the male/female antithesis (one of the cardinal Pythagorean opposites), may allude to the ultimately prophetic descent of Pythagorean wisdom. Aristoxenus maintained that Pythagoras took his doctrines (or, at least, the "moral" ones) from Themistoclea from Delphi: D.L. VIII, 21: ὁ δ' αὐτός φησιν (sc. Aristoxenus), ...καὶ τὰ δόγματα λαβεῖν αὐτὸν παρὰ τοῖς ἐν Δελφοῖς Θεμιστοκλείας. And §8: φησὶ δὲ καὶ Ἀριστόξενος τὰ πλεῖστα τῶν ἡθικῶν δογμάτων λαβεῖν τὸν Πυθαγόραν παρὰ Θεμιστοκλείας τῆς ἐν Δελφοῖς. Themistocleia is another, and "previous", Diotima.

3) In Orphism, the religious significance of remembrance (Μνημοσύνη) is heavy, esp. in an eschatological context. In general, as in every doctrinal religion, salvation depends on truth and knowledge of truth. Such knowledge has to be actual, in order to be active, not merely potential. And this condition is expressed by memory: one *knows the truth*, when one *recognises* it in being, and, thus, when one *remembers ιτ. Recognition* is of the essence of knowledge, and this is why *remembrance is the criterion of its possession*. (This is, in fact, the source of the Phaedonian development of the doctrine of ἀνάμνησις).

This experience of remembrance as constitutive of the knowledge of truth is found symbolised in Orphism within the context of the powerful imagery regarding what happens to the soul upon the death of man. We possess a few variants of this representation in the gold leaves discovered appended to the corpses

in burials from various places in Italy and Greece. These gold leaves provide the ritualistic confession of a soul on the process of divinization. When she leaves the light of sun (Ἀλλ' ὁπόταμ ψυχὴ προλίπη φάος Άελίοιο, A₄ 1 (Zuntz)) and comes before the palaces of Hades, she will find (B1 and B2 Zuntz and cf. B3-8) two sources of water, one to the left by a white cypress, the other further on to the right, coming from the Lake of Remembrance. (There is a complication in that B2 from Pharsalus seems to locate the first spring to the right as well - $\partial \delta \xi_{I} \alpha$ -, but I think the basic pattern should be the one I indicated above). The initiated soul should refrain from drinking water from the former source. But the soul is dry from death and suffers having been cut off from the juices of life. Before the right source there stand Guardians who ask her to identify herself. They want one answer: "Τῆς παῖς εἰμι καὶ Οὐοανοῦ ἀστερόεντος· αὐτὰρ ἐμοὶ γένος οὐράνιον· τόδε δ' ἴστε καὶ αὐτοί". The Zagreus story is implicitly contained here, as is evidenced by the entire extant corpus of similar leaves. Drinking from the water of Mnemosyne the soul clears her intellectual vision, sees truth in its wholeness and is saved: she escapes from the cycle of necessity and enters divine Elysium. She is free from the bondage of rebirth and redeath.

The Pythagoreans elaborated this basic religious, eschatological experience into their systematic and "logical" treatment of reality.

First, it is memory of previous reincarnations that comes into the picture, closer to the religious domain. To remember one's

previous lifes on earth, is a titanic feat of remembrance. Pythagoras was conscious of them. There are two known chief accounts of Pythagoras' preincarnations. One was given by a group of Pythagoreans and writers on Pythagoreanism: Androcydes, Eubulides, Aristoxenus, Hippobotus and Neanthes. Theol. Arithmeticae, pp. 52.8-53.10 = 14DK A8. They held that the reincarnations of Pythagoras' soul were observing a period of 216 years = 6^3 , a number expressing psychogonic revitalization. They further reckoned that this fits well with the widespread notion that Pythagoras had lived before as Euphorbus during the Trojan war. The other account, reported by Heracleides Ponticus (Fr. 89 Wehrli – followed probably by Dicaearchus (Fr. 36 Wehrli) and Clearchus (Fr. 10 Wehrli)), gives a more continuous series of multiple incarnations, starting with Aethalides, the son of Mercury. The god of λόγος granted him memory of all things acquainted with: τὸν δ' Ἑρμῆν εἰπεῖν αὐτῷ ἐλέσθαι ὅτι ἂν βούληται πλὴν ἀθανασίας. αἰτήσασθαι οὖν ζωντα καὶ τελευτωντα μνήμην ἔχειν των συμβαινόντων. ἐν μὲν οὖν τῆ ζωῆ πάντων διαμνημονεῦσαι, ἐπεὶ δὲ ἀποθάνοι, τηρῆσαι τὴν αὐτὴν μνήμην. The soul of Aethalides thus knew ώς περιεπολήθη καὶ εἰς ὄσα φυτὰ καὶ ζῷα (notice the plant-incarnations as in Empedocles) παρεγένετο καὶ ὅσα ἡ ψυχὴ ἐν τῷ Ἅιδη ἔπαθε καὶ αἱ λοιπαὶ τίνα ύπομένουσιν. After a stated sequence of transmigrations, the soul γενέσθαι Πυθαγόραν καὶ πάντων τῶν εἰρημένων μεμνῆσθαι. Here we have the initial formulation of the cruder idea, memory of all particular things and events with which the soul had been acquainted on Earth and in Hades: ἄτε οὖν ἡ ψυχὴ ἀθάνατός τε οὖσα

καὶ πολλάκις γεγονυῖα, καὶ ἐωρακυῖα καὶ τὰ ἐνθάδε καὶ τὰ ἐν Ἅιδου καὶ πάντα χρήματα, οὐκ ἔστιν ὅτι οὐ μεμάθηκεν, Meno, 81c5-7. (The particularity of the memory and reminiscence in this first Platonic formulation of the doctrine is, therefore, explicable).

Second, such particularism in knowledge was early sublated, within the framework of the Pythagorean systematic and "principled' thinking, to more general formulations. "The whole truth about souls" was a first step towards such generalizations. So, again Heracleides Ponticus reports the story of Empedotimus, of whom it is said that θηρῶντα μετ' ἄλλων ἐν μεσημβοία σταθεοᾶ κατά τινα χῶρον αὐτὸν ἔρημον ἀπολειφθέντα λέγων τῆς τε τοῦ Πλούτωνος ἐπιφανείας τυχόντα καὶ τῆς Περσεφόνης καταλαμφθῆναι μὲν ὑπὸ τοῦ φωτὸς τοῦ περιθέοντος κύκλω τοὺς θεούς, ἰδεῖν δὲ δι' αὐτοῦ πᾶσαν τὴν περὶ ψυχῶν ἀλήθειαν ἐν αὐτόπτοις θεάμασιν (Fr. 93 Wehrli). Empedotimus gave a cosmology as well to suit his revealed psychology; cf. Fr. 95-96 Wehrli. (No wonder the soul-light theory was Heracleides').

Third. Particularism in memorizing was cultivated to a phenomenal degree, and systematized, by specific practices. Such a method consisted in trying to remember every morning, before rising from the bed of sleep, what exactly happened the day before in the sequence in which every singular event occurred. And the same endeavour was attempted for the serial happenings of the previous day, and the one before, and so on. Iamblichus *Vita Pyth*. §165 (= 58DK D1 p. 467.23 sqq.): Πυθαγόρειος ἀνὴρ οὐ πρότερον ἐκ τῆς κοίτης ἀνίστατο ἢ τὰ χθὲς γενόμενα πρότερον ἀναμνησθείη.

ἐποιεῖτο δὲ τὴν ἀνάμνησιν τόνδε τὸν τρόπον. ἐπειρᾶτο ἀναλαμβάνειν τῆ διανοία, τί πρῶτον εἶπεν ἢ ἤκουσεν ἢ προσέταξε τοῖς ἔνδον ἀναστὰς καὶ τί δεύτερον καὶ τί τρίτον, καὶ περὶ τῶν ἐσομένων ὁ αὐτὸς λόγος· καὶ πάλιν αὖ ἐξιὼν τίνι πρώτω ἐνέτυχε καὶ τίνι δευτέρω, καὶ λόγοι τίνες ἐλέχθησαν πρῶτοι καὶ δεύτεροι καὶ τρίτοι, καὶ περὶ τῶν ἄλλων δὲ ὁ αὐτὸς λόγος. πάντα γὰρ ἐπειρᾶτο ἀναλαμβάνειν τῆ διανοία τὰ συμβάνα ἐν ὅλη τῆ ἡμέρα, οὕτω τῆ τάξει προθυμούμενος ἀναμιμνήσκεσθαι, ὥς ποτε συνέβη γενέσθαι ἕκαστον αὐτῶν. εἰ δὲ πλείω σχολὴν ἄγοι ἐν τῷ διεγείρεσθαι, καὶ τὰ <κατὰ τὴν>τρίτην ἡμέραν συμβάντα τὸν αὐτὸν τρόπον ἐπειρᾶτο ἀναλαμβάνειν. In this mnemonic technique the temporal connectedness of the events helps the faculty of memory to recall them in their particularity.

Pythagoreans laid primary stress on the power of memory. Its exercise was pursued through various techniques. They considered it the greatest asset for scientific knowledge and expertise and practical wisdom (applied knowledge). Op. cit., §166: καὶ ἐπὶ πλέον ἐπειρῶντο τὴν μνήμην γυμνάζειν οὐδὲν γὰρ μεῖζον πρὸς ἐπιστήμην καὶ ἐμπειρίαν καὶ φρόνησιν τοῦ δύνασθαι μνημονεύειν. They soon would develop a theoretical account for such an emphasis on memory and mnemonic techniques in the pursuit of higher science. The main point was the recognition on the part of the thinking subject that it is one and the same faculty in man which possesses knowledge and keeps right judgement on the one hand, and which learns and remembers on the other. By cultivating therefore the power of remembrance you ipso facto cultivate the power of knowing and judging correctly. Op. cit. 164: ῷοντο δὲ δεῖν κατέχειν καὶ διασφζειν ἐν τῆ μνήμη πάντα τὰ διδασκόμενά τε καὶ φραζόμενα, καὶ μέχρι τούτου

συσκευάζεσθαι τάς τε μαθήσεις καὶ τὰς ἀκοράσεις, μέχρι ὅτου δύναται παραδέχεσθαι τὸ μανθάνον καὶ διαμνημονεῦον, ὅτι ἐκεῖνό ἐστιν ῷ δεῖ γιγνώσκειν καὶ ἐν ῷ γνώμην φυλάσσειν. ἐτίμων γοῦν σφόδοα τὴν μνήμην καὶ πολλὴν αὐτῆς ἐποιοῦντο γυμνασίαν τε καὶ ἐπιμέλειαν, ἔν τε τῷ μανθάνειν οὐ πρότερον ἀφιέντες τὸ διδασκόμενον, ἕως περιλάβοιεν βεβαίως τὰ ἐπὶ τῆς πρώτης μαθήσεως. Knowledge was intimately associated to learning. They secured knowledge as permanent possession in human soul by (in the words of Iamblichus they would not leave the object of learning till they have achieved) the firm and certain comprehension of what exactly constituted the initial learning of it. (This was speculatively extended to the vicissitudes of soul in her eternal life).

Iamblichus testimony stems from Aristoxenus' Pythagorean works ($\Pi v \theta \alpha \gamma o \rho \iota \kappa \alpha \iota$ ἀποφάσεις and $\Pi \varepsilon \rho \iota$ $\Pi v \theta \alpha \gamma o \rho \iota \kappa o \tilde{v}$ (or $\Pi v \theta \alpha \gamma o \rho \varepsilon (o v)$) βίου).

Fourth. Finally, in the theorization of mnemonic particularism which the Pythagoreans cultivated as a way to certain knowledge, there was a last stage which was grounded on the ultimate bringing together of the two most characteristic tenets of Pythagoreanism. Thus Porphyry (drawing from Dicaearchus): μάλιστα μέντοι γνώριμα παρὰ πᾶσιν ἐγένετο πρῶτον μὲν ὡς ἀθάνατον εἶναί φησι τὴν ψυχήν, εἶτα μεταβάλλουσαν εἰς ἄλλα γένη ζώων, πρὸς δὲ τούτοις ὅτι κατὰ περιόδους τινὰς τὰ γενόμενά ποτε πάλιν γίνεται, νέον δ΄ οὐδὲν ἀπλῶς ἔστι, καὶ ὅτι πάντα τὰ γινόμενα ἔμψυχα ὁμογενῆ δεῖ νομίζειν. φαίνεται γὰρ εἰς τὴν Ἑλλάδα τὰ δόγματα πρῶτος κομίσαι ταῦτα Πυθαγόρας (Porphyry, Vita Pyth., 18 = DK 14 A 8a. In Wehrli's Dikaearchos there appears §18 of Porphyry's Vita Pyth. as Fr. 33, but unaccountably the

following passage §19 is ommitted). The doctrine of the eternal recurrence of identical world-cycles is early Pythagorean on good evidence. Besides Dicaearchus, Eudemus also elaborates on it, Fr. 88 Wehrli (from Simplicius quoting *verbatim* the old Peripatetic: εἰ δέ τις πιστεύσειε τοῖς Πυθαγορείοις, ὤστε πάλιν τὰ αὐτὰ ἀριθμῷ, κἀγὼ μυθολογήσω τὸ οαβδίον ἔχων ὑμῖν καθημένοις οὕτω, καὶ τὰ ἄλλα πάντα όμοίως έξει, καὶ τὸν χρόνον εὔλογόν ἐστι τὸν αὐτὸν εἶναι etc. Theopompus and Eudemus ascribed to the idea a Magian origin (Eudemus Fr. 89 Wehrli): δς (ss. Θεόπομπος) καὶ ἀναβιώσεσθαι κατὰ τοὺς Μάγους φησὶ τοὺς ἀνθρώπους καὶ ἀθανάτους ἔσεσθαι, καὶ τὰ ὄντα ταῖς αύτῶν περικυκλήσεσι διαμενεῖν ταῦτα δὲ καὶ Εὔδημος ὁ Ρόδιος ίστορεῖ. (αὐτῶν περικυκλήσεσι rather than αὐτῶν ἐπικλήσεσι as in Jacobi Fr.Gr.H. 115 F64). Temporal sequence is not accidental: it repeats itself in its entirety sempiternally, and this must be for some reason. We are here moving into the archaic antecedens of Stoicism. Elsewhere Ι have proposed candidate for the Pythagoreo/Heracleteian fusion required to generate the conception of a World unfolding itself according to a fixed law of development constituting a cyclic pattern. (A.L. Pierris, The Origin of Stoic Fatalism, esp. pp. 27-30, in *Chypre et les Origines du Stoicism*, Actes du Colloque Paris 12-13 Mai 1995, Publications du Centre Cultural Hellénique de Paris, 1996, pp. 21-30).

4) We have reached, in the previous section, the stage, where it appears that the idea of an ordered pattern of things is indeed implicated in the Pythagorean "Memorism". But there is much more

in Pythagoreanism by way of cohesiveness and systematicalness than this rather loose implication. In the midst of Socrates' application of the doctrine of transmigration to the question of the possibility of learning (and thus of the possibility of real knowledge), we meet an unprepared, strong statement of the "kinship of nature": ἄτε γὰρ τῆς φύσεως ἀπάσης συγγενοῦς οὔσης etc. (Meno, 81c9-d1). The statement is a crucial link in the demonstration that there can be learning and scientific knowledge of diverse things. For the fact that all truth is implicit in the soul (because through the eternal recycling she has "seen" visually and mentally everything of this and the other world) is not by itself sufficient to establish the real possibility of actual knowledge. What Socrates achieves by his invocation of the "kinship of all nature" doctrine is to show that once a single individual truth has been secured, all truth can in principle be obtained: ἄτε γὰο τῆς φύσεως ἀπάσης συγγενοῦς οἴσης, καὶ μεμαθηκυίας τῆς ψυχῆς ἄπαντα, οὐδὲν κωλύει εν ἀναμνησθέντα -δ δὴ μάθησιν καλοῦσιν ἄνθρωποι -τἆλλα πάντα αὐτὸν ἀνευρεῖν, ἐάν τις ἀνδοεῖος ἦ καὶ μὴ ἀποκάμη ζητῶν· τὸ γὰο ζητεῖν ἄρα καὶ τὸ μανθάνειν $\dot{\alpha}$ νάμνησις ὅλον ἐστίν (81c9 – d5). It is now only a question of perseverance – and time, if not one life's then of more. The point is of immense consequence: either no actual knowledge, or, in principle, absolute *knowledge of reality.*

[The thesis is made the object of a brilliant burlesque in the *Euthydemus*. 293b1-297b1. The two sophist-brothrs engage in an exhibition of negative dialectics, or eristics, the offspring of Eleatism. Plato wants to show what havoc "strict thinking" can effect in the

human quest of truth, if *strictly* pursued and applied. Euthydemus and Dionysiodorus argue on eristical grounds that εἴπες εν ἐπίσταμαι, ἄπαντα ἐπίσταμαι (293d5); moreover, that πάντες πάντα ἐπίστανται, εἴπες καὶ ἕν (294a10); furthermore, that not only one knows everything, if he knows anything, but also he always (καὶ ἀεί) knew everything (294e8; 295a8); and finally we reach in this *crescendo* the remarkable view that καὶ πρὶν αὐτὸς γενέσθαι, καὶ πρὶν οὐρανὸν καὶ γῆν γενέσθαι, ἠπίστω ἄπαντα, εἴπες ἀεὶ ἐπίστασαι. καὶ ναὶ μὰ Δία, ἔφη, αὐτὸς ἀεὶ ἐπιστήση καὶ ἄπαντα, ἄν ἐγὼ βούλωμαι (296d1-4).

Eristics is founded on Eleatic thinking absolutism, giving the wrong turn to it. the general pattern of inference can be put thus: if x is A, x is. If x is, x is Y (where Y is any (putatively) real content of being). Socrates repeatedly intimates the error of this procedure, in the course of the above argument. But he also explains the point of such eristics: it is preliminary preparation of the ground for the serious and important thing (277d1-278e1). This projected estimate on the part of Socrates, is offered after another show of "logical" derivations of puzzling absurdities, earlier in the dialogue, by the expert brothers. Interestingly enough, among that set of $\check{\alpha}$ τοπ α is the demonstration that one has to negate both alternatives to the question π ότερον οί μανθάνοντες μανθάνουσιν $\mathring{\alpha}$ ἐπίστανται $\mathring{\eta}$ $\mathring{\alpha}$ μ $\mathring{\eta}$ ἐπίστανται; (276d7-8 and sqq.).]

The cohesion of knowledge is clearly grounded on the kinship of nature: ἄτε γὰο τῆς φύσεως ἁπάσης συγγενοῦς οὔσης etc. - because nature is in its entirety kindred etc. Now kinship connotes common progeny, the same (pro)genitors. That the natural world has all of it

the same "ancestors", means philosophically that it proceeds from the same ultimate duality of principles, which function in biological terms as the primeval conjugation of male and female. This all assumes its most forceful significance in connection with the Pythagorean theory of world-formation out of the conjunction of the two primary opposites, $\pi \dot{\epsilon} \rho \alpha \zeta$ and $\ddot{\alpha} \pi \epsilon \rho \rho \nu$. Thus, e.g., in Philolaus, 44DK Β1: ά φύσις δ' ἐν τῷ κόσμῳ άρμόχθη ἐξ ἀπείρων τε καὶ περαινόντων, καὶ ὅλος <ό> κόσμος καὶ τὰ ἐν αὐτῷ πάντα. Philolaus explained that the dissimilar and alien natures of the two principles needed a supervening harmonious mixture or conjugation in order to bring forth the κόσμος, ordered existence: ἐπεὶ δὲ ταὶ ἀρχαὶ ύπᾶρχον οὐχ ὁμοῖαι οὐδ' ὁμόφυλοι ἔσσαι, ἤδη ἀδύνατον ἦς κα αὐταῖς κοσμηθηναι, εἰ μὴ άρμονία ἐπεγένετο ῷ τινιῶν ἄδε τρόπω ἐγένετο. τὰ μὲν ὧν ὁμοῖα καὶ ὁμόφυλα άρμονίας οὐδὲν ἐπεδέοντο, τὰ δὲ ἀνόμοια μηδὲ ὁμόφυλα μηδὲ ἰσοταγῆ ἀνάγκα τῷ τοιαύτᾳ ἁομονίᾳ συγκεκλεῖσθαι, οἵα μέλλοντι ἐν κόσμω κατέχεσθαι (44 DK B6). This harmonious conjugation brings integration and unity into the outcome: ἔστι γὰο άρμονία πολυμιγέων ἕνωσις καὶ δίχα φρονεόντων συμφοόνησις (B10). Number (the carrier of harmony) makes things related (kindred) to each other and knowable. Kinship and knowability of reality go hand in hand in Pythagoreanism: γνωμικὰ γὰο ά φύσις ά τῷ ἀριθμῷ καὶ ἡγεμονικὰ καὶ διδασκαλικὰ τῷ ἀπορουμένω παντὸς καὶ ἀγνοουμένω παντί. οὐ γὰρ ἦς δῆλον οὐδενὶ οὐδὲν τῶν πραγμάτων οὔτε αὐτῶν ποθ' αὑτὰ οὔτε ἄλλω πρὸς ἄλλο, εἰ μὴ ἦς ἀριθμὸς καὶ ά τούτω οὐσία. νῦν δὲ οὖτος καττὰν ψυχὰν άρμόζων αἰσθήσει πάντα γνωστὰ καὶ ποτάγορα ἀλλάλοις κατὰ γνώμονος φύσιν ἀπεργάζεται σωματῶν καὶ σχίζων τοὺς λόγους χωρὶς ἑκάστους τῶν

πραγμάτων των τε ἀπείρων καὶ των πεπερασμένων (B11, which see, the whole of it). Thus number is the conquering and self-subsisting cohesion of the eternal stay of things temporal and this-worldly alike: ἀριθμὸν εἶναι τῆς τῶν κοσμικῶν αἰωνίας διαμονῆς κρατιστεύοισαν καὶ αὐτογενῆ συνοχήν, B23 (deemed spurious by Diels-Kranz, but which sounds Philolaean in substance if not in phrazing). Αὐτογενῆ may even here mean kindred, as in Aeschylus, Suppl. 8, if indeed this is the right reading there. The idea finds a similar, in fact parallel, expression in another reputedly spurious fragment (B21), which again, however, seems to preserve, in the relevant part at least, sound Philolaean doctrine: the world is indestructible and eternal; ἀλλ' ἦν ὅδε ὁ κόσμος ἐξ αἰῶνος καὶ εἰς αὶῶνα διαμενεῖ, εῖς ὑπὸ ἑνὸς τῷ συγγενέος καὶ κρατίστω καὶ ανυπερθέτω κυβερνώμενος. This kindred and most powerful principle is immanent in it, the principle of harmony, that is divine number.

Talk of kindredness refers to the biological ("hylozoistic") model of conceiving reality in protorationality. Thus male and female form indeed one of the ten fundamental expressions of the primal contrariety in the list of Pythagorean syzygies according to Aristotle (*Met.* 986a22-26).

Plato utilises the same biological terminology to clarify the constitution of this world of becoming from its principles: ἐν δ' οὖν τῷ παρόντι χρὴ γένη διανοηθῆναι τριττά, τὸ μὲν γιγνόμενον, τὸ δ' ἐν ῷ γίγνεται, τὸ δ' ὅθεν ἀφομοιούμενον φύεται τὸ γιγνόμενον. Καὶ δὴ καὶ προσεικάσαι πρέπει τὸ μὲν δεχόμενον μητρί, τὸ δ' ὅθεν πατρί, τὴν δὲ

μεταξὺ τούτων φύσιν ἐκγόνω etc. *Timaeus*, 50c-d. Nature that grows out of its principles is like the offspring of its parents. All (natural) existence is thus kindred: it comes from the common couple of ancestors, π έρας and ἄ π ειρον, directly or through intermediation. In *Philebus*, similarly, natural reality is described as an offspring of π έρας and ἄ π ειρον, the becoming into substance (i.e. the φύσις) of things: ἀλλὰ τρίτον φάθι με λέγειν, εν τοῦτο τιθέντα τὸ τούτων (sc. of π έρας and ἄ π ειρον) ἔκγονον ἄ π αν, γένεσιν εἰς οὐσίαν ἐκ τῶν μετὰ τοῦ πέρατος ἀ π εργασμένων μέτρων (26d7-9).

Behind, and at the root of, all this lies as usual a religiously formulated experience. Thus Pindar (again) *Nem.* VI, 1-7:

εν ἀνδοῶν, εν θεῶν γένος· ἐκ μιᾶς δὲ πνέομεν ματοὸς ἀμφότεοοι· διεγείρει δὲ πᾶσα κεκριμένα δύναμις, ὡς τὸ μὲν οὐδέν, ὁ δὲ χάλκεος ἀσφαλὲς αἰὲν ἕδος μένει οὐρανός. ἀλλά τι προσφέρομεν ἔμπαν ἢ μέγαν νόον ἤτοι φύσιν ἀθανάτοις etc.

Common maternal parenthood between gods and men, means the origin of both from Earth (and Heavens). We meet once more in these ideas of kindrednesses the account of the Titanic origin of manhood, i.e. *OrphicoPythagorean wisdom*.

5) But the real point of all this context – analysis is what bearing it has on Platonic *dialectics*. The Pythagorean "kinship of nature" doctrine is founded on the "mathematical" derivation of all reality from the dual principles of $\pi \acute{\epsilon} \varrho \alpha \varsigma$ and $\check{\alpha} \pi \epsilon \iota \varrho \circ \nu$. On its turn,

the doctrine grounds the "cohesion of knowledge" conception. This again entails that truth can, in principle, be unfolded methodically in its entirety, once a single piece of certain knowledge has been established. But the paradigm case of indubitable knowledge is mathematics. Hence the process of philosophical learning (i.e. of dialectis as the road to absolute truth) must start at mathematical theory. This is why Socrates in the Meno provides and example of proper essential definition (and as an example it was explicitly adduced: ...πειοω εἰπεῖν, ἵνα καὶ γένηταί σοι μελέτη ποὸς τὴν πεοὶ τῆς ἀρετῆς (and of everything else) ἀπόκρισιν, Meno, 75a8-9) by asking the τί ἐστιν question of *shape* (and, furthermore, associates with it the apparently non-mathematical concept of colour, which, however, was somehow reduced in Pythagoreanism to, (or, alternatively, was the reduction-basis of, or, at any rate, was essentially connected to) surface bounding a solid form, i.e. to shape). And this is, more importantly, why Socrates here gives an example of learning by "demonstrating" a mathematical theorem – and one in fact which is directly related to the (in)famous Pythagorean discovery of the incommensurability of the diagonal of a square with its side. Demonstration consisting in the eliciting of truth out of the learner's mind through an appropriate framework of questioning. Thus we have in effect the essence according to Plato of the *Socratic probing*. Elenchus consists in the methodical way of rendering knowledge explicit, of activating truth out of its slumbering status in human mind. In this elenctic process, the mind of the learner passes from a condition in which it thinks it knows but in reality is ignorant, to a

state of $\dot{\alpha}\pi$ ogí α in which it recognizes its ignorance. Then elenchus turns positive, the mind having been cleared from its false beliefs and rendered receptive to truth: now truth can be recognized as such and the state of knowledge achieved (84a3-d2). Certainly, in order for such truth to be stabilized as an exact and permanent possession of mind, repeated and systematic testing is necessary: καὶ νῦν μέν γε αὐτ $\tilde{\omega}$ (i.e. in this first awakening of truth in the slave-boy's mind) ώσπες ὄνας ἄςτι ἀνακεκίνηνται αί δόξαι αὖται· εἰ δὲ αὐτόν τις άνερήσεται πολλάκις τὰ αὐτὰ ταῦτα καὶ πολλαχῆ, οἶσθ' ὅτι τελευτῶν οὐδενὸς ἦττονἀκριβῶς ἐπιστήσεται περὶ τούτων (85c9-d1). This is very close to the Pythagorean insistence on repeated checking with a view to secure comprehension of what was involved in the first awaking of (a given) truth in the mind: ἔν τε τῷ μανθάνειν οὐ πρότερον ἀφιέντες τὸ διδασκόμενον, ἕως περιλάβοιεν βεβαίως τὰ ἐπὶ τῆς πρώτης μαθήσεως (88 DK, D1 [from Aristoxenus] p. 467.21-2). Through the positive questioning, what the mind contained as latent knowledge and, at most, actual true belief ($\dot{\alpha}$ ληθής δόξα), becomes scientific knowledge: ἐνέσονται αὐτῷ (sc. τῷ ἀνθρώπω) ἀληθεῖς δόξαι, αῖ έρωτήσει ἐπεγερθεῖσαι ἐπιστῆμαι γίγνονται (86a7-8). This rousing of truth in the mind by means of appropriate examination implies that the truth of being exists always in the soul: $\dot{\alpha}$ εὶ ἡ $\dot{\alpha}$ λήθεια ἡμῖν τῶν ὄντων ἐστὶν ἐν τῆ ψυχῆ (86b1-2). [Which again can be used to prove the immortality of the soul (86b2), - something announced in anticipation to the full development of the idea in the Phaedo, a dialogue to which Meno is clearly meant to serve in this respect as a preliminary].

Having now reached this stage, we may drop, if we feel inclined to do so, the ladder by which we ascended as far: the religious roots and formulations of these doctrines can be left out of the picture on suspension: $\kappa\alpha$ ὶ τὰ μέν γε ἄλλα οὐκ ἂν πάνυ ὑπὲο τοῦ λόγου διϊσχυοισαίμην (86b6-7). So much, however, is clear: with secure anchorage in mathematics, all truth of being can in principle be revealed (in substance, b7-c2).

6) Mathematical truth is not only the best starting point from which to elicit the entire truth of being. It also provides the methodology to do this. In the Meno (86d3-87c2), the pattern is taken from the mathematical solution of geometrical problems. The question is to determine whether a given, particular object has the property A. And one shows that x will be A if x is B. This procedure depends on establishing the relationship B \rightarrow A. In the *Phaedo* it is this drawing of conclusions from premises which are taken for granted in the given connection, that is called argument ex hypothesi. In this respect *Phaedo* stands to *Meno* in the same relationship as regards this systematically ambiguous employment of the terminology "hypothetical reasoning", as with the utilization of the doctrine of ἀνάμνησις: here it is coloured by particularism, while in the *Phaedo* it is refined into the recollection of the idea of things which we perceive as (more or less) determined by the idea (as instances of the idea).

Hypothetical argument in the generalized sense relies on the principle of logical (and ontological) *coherence. Phaedo* 100a3-7: καὶ

ύποθέμενος έκάστοτε λόγον ον αν κρίνω έρρωμενέστατον είναι, α μεν ἄν μοι δοκῆ τούτω συμφωνεῖν τίθημι ώς ἀληθῆ ὄντα, καὶ περὶ αἰτίας καὶ περὶ τῶν ἄλλων ἁπάντων [ὄντων], ἃ δ' ἂν μή, ὡς οὐκ ἀληθῆ. The hypothesis of one argument, may become the conclusion of another, which goes more deeply into the nature of reality. But one should exhaust first all relevant inferences from the given hypothesis (Phaedo, 101d1-e3): ...ἐχόμενος ἐκείνου τοῦ ἀσφαλοῦς τῆς ὑποθέσεως, οὕτως ἀποκρίναιο ἄν. εἰ δέ τις αὐτῆς τῆς ὑποθέσεως ἔχοιτο, χαίρειν έψης ἂν καὶ οὐκ ἀποκρίναιο ἕως ἂν τὰ ἀπ' ἐκείνης ὁρμηθέντα σκέψαιο εἴ σοι ἀλλήλοις συμφωνεῖ ἢ διαφωνεῖ· ἐπειδὴ δὲ ἐκείνης αὐτῆς δέοι σε διδόναι λόγον, ώσαύτως ἂν διδοίης, ἄλλην αὖ ὑπόθεσιν ὑποθέμενος ήτις τῶν ἄνωθεν βελτίστη φαίνοιτο, ἔως ἐπί τι ἱκανὸν ἔλθοις, ἄμα δὲ οὐκ ἂν φύροιο ὤσπερ οἱ ἀντιλογικοὶ περί τε τῆς ἀρχῆς διαλεγόμενος καὶ τῶν ἐξ ἐκείνης ὡρμημένων, εἴπερ βούλοιό τι τῶν ὄντων εύρεῖν. Of course, one should test again and again to clarify the (logical) relationships, and make them certain (*Phaedo*, 107b).

The hypothetical argumentation is, however, described by Socrates in the renowned methodological excursus of *Phaedo* as $\delta\epsilon\dot{\nu}\tau\epsilon\varphi\circ\kappa$ $\pi\lambda\circ\tilde{\nu}\varsigma$ (99c9-d1), something one embarks at having failed to comprehend the causal working of the principle of Goodness ($\tau\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ $\dot{\nu}$ in the world. *Since this argumentation involves also the postulation of the full-blown ideas, it follows that the theory of ideas cannot be Plato's ultimate explanation of reality.* In the *Republic*, we are told in detail what is missing. *First*, it is a question of moving in the reverse direction from that of a genuinely philosophical (i.e. dialectical) investigation: instead of drawing conclusions from premised

hypotheses, one must ascend the ladder of logical and ontological presupposition towards the absolutely ἀνυπόθετον. ΣΤ, 510b4-9: ἦ τὸ μὲν αὐτοῦ τοῖς τότε μιμηθεῖσιν ὡς εἰκόσιν χρωμένη ψυχὴ ζητεῖν αναγκάζεται έξ ύποθέσεων, οὐκ ἐπ' ἀρχὴν πορευομένη ἀλλ' ἐπὶ τελευτήν, τὸ δ' αὖ ἕτερον - τὸ ἐπ' ἀρχὴν ἀνυπόθετον - ἐξ ὑποθέσεως ιοῦσα και ἄνευ τῶν περὶ ἐκεῖνο εἰκόνων, αὐτοῖς εἴδεσι δι' αὐτῶν τὴν μέθοδον ποιουμένη. The conjuncton of downwards inferential movement with the use of images is not necessary, as I have indicated above; and similarly with the upwards movement and pure thought. On the other hand "dialectics" cannot essentially utilize exemplification and instantiation. In fact dialectics consists in the thought-process through which one ascends to the $\dot{\alpha}$ νυπόθετον principle of being and then descends orderly in all articulate variation of reality: ... ὁ λόγος ἄπτεται τῆ τοῦ διαλέγεσθαι δυνάμει (sc. the intelligible in strict sense), τὰς ὑποθέσεις ποιούμενος οὐκ ἀρχὰς άλλὰ τῷ ὄντι ὑποθέσεις, οἷον ἐπιβάσεις τε καὶ ὁρμάς, ἵνα μέχρι τοῦ άνυποθέτου ἐπὶ τὴν τοῦ παντὸς ἀρχὴν ἰών, ἁψάμενος αὐτῆς, πάλιν αὖ έχόμενος τῶν ἐκείνης ἐχομένων, οὕτως ἐπὶ τελευτὴν καταβαίνη, αἰσθητῷ παντάπασιν οὐδενὶ προσχρώμενος, ἀλλ' εἴδεσιν αὐτοῖς δι' αὐτῶν εἰς αὐτά, καὶ τελευτῷ εἰς εἴδη, 511b3-c2 (cf. c4-d2).

Secondly, and chiefly, in book Z, Plato offers a first level description of dialectics. The foundation is provided by the mathematical "sciences" (not strictly science, ἐπιστήμη, yet not mere true belief, ὀϱθὴ δόξα, but intelligence in between, διάνοια). This is developed in 525a-531c. One should then concentrate on what is common to the various mathematical branches (531c9-d4). If this is

done with a view to reaching to the ἀνυπόθετον, we have dialectics (cf. 531d5-532a5) esp. 532a5-b4: οὕτω καὶ ὅταν τις τῷ διαλέγεσθαι ἐπιχειοῆ ἄνευ πασῶν τῶν αἰσθήσεων διὰ τοῦ λόγου ἐπ' αὐτὸ ὁ ἔστιν έκαστον όρμᾶν, καὶ μὴ ἀποστῆ πρὶν ἂν αὐτὸ ὁ ἔστιν ἀγαθὸν αὐτῆ νοήσει λάβη, ἐπ' αὐτῷ γίγνεται τῷ τοῦ νοητοῦ τέλει, ὥσπερ τότε ἐπὶ τῷ τοῦ ὁρατοῦ (referring back to 507c10-509c2). Παντάπασιν μεν οὖν, ἔφη. -Τί οὖν; οὐ διαλεκτικήν ταύτην τήν πορείαν καλεῖς; Mathematics becomes dialectical when it searches for first principles (533b1-e2); esp. 533c7-d7: ...ή διαλεκτική μέθοδος μόνη ταύτη πορεύεται, τὰς ὑποθέσεις ἀναιροῦσα, ἐπ' αὐτὴν τὴν ἀρχὴν ἵνα βεβαιώσηται ... ας (sc. mathematical disciplines) ἐπιστήμας μὲν πολλάκις προσείπομεν διὰ τὸ ἔθος, δέονται δὲ ὀνόματος ἄλλου, ἐναργεστέρου μὲν ἢ δόξης, ἀμυδροτέρου δὲ ἢ ἐπιστήμης -διάνοιαν δὲ αὐτὴν ἔν γε τῷ πρόσθεν που ὡρισάμεθα etc. Once the ἀνυπόθετον has been reached and the idea of goodness made the pivot of mathematics, elenchus takes up its positive aspect: ος αν μή ἔχη διορίσασθαι τῷ λόγῳ ἀπὸ τῶν ἄλλων πάντων ἀφελὼν τὴν τοῦ ἀγαθοῦ ίδέαν, καὶ ὤσπερ ἐν μάχη διὰ πάντων ἐλέγχων διεξιών, μὴ κατὰ δόξαν άλλα κατ' οὐσίαν προθυμούμενος ἐλέγχειν, ἐν πάσι τούτοις ἀπτῶτι τῷ λόγω διαπορεύηται, etc. (534b8-c3). Thus dialectics is the θοιγκὸς τοῖς μαθήμασιν and their τέλος (534e2-535a1).

I have maintained and argued for elsewhere the essential coherence between the programatic description of higher philosophy in the *Republic* and the *Laws* on the one hand, and between that programme and the reputed carrying it out in the Unwritten Doctrines (and in the discourse $\pi \epsilon \varrho i \tau o \tilde{\nu} \dot{\alpha} \gamma \alpha \theta o \tilde{\nu}$) on the other,. [V. A.L. Pierris, *The Metaphysics of Politics in the Politeia, Politikos and*

Nomoi Dialogue Groups, in A. Havlicek – F. Karfik (eds.) *The Republic and the Laws of Plato*, Proceedings of the First Symposium Platonicum Pragense, pp. 117-145, esp. pp. 120-126, 130 sqq.].

7) In the final section of the *Meno* we have the inimitable daedalic similitude: true beliefs exist side by side with false ones in the soul of the unphilosophical (= undialectic) vulgar. For as long as they are entertained by the mind (for as long as they lay hold of it), no harm is being done by the fact that they do not still constitute proper scientific knowledge: $\kappa\alpha$ ì γὰρ αἱ δόξαι αἱ ἀληθεῖς, ὅσον μὲν ἄν χρόνον παραμένωσιν, καλὸν τὸ χρῆμα καὶ πάντ' ἀγαθὰ ἐργάζονται (97e6-98a1. Cf. 97a9-c10). [It is a different matter, whether the condition of true belief is empirically distinguishable from the state of real knowledge. The answer lies, for Plato, in the affirmative. For true beliefs lack the systematical cohesion and ultimate dependence on first principles that scientific knowledge possesses].

True belief, however, is not permanent possession of mind, being intrinsically unstable – exactly by virtue of its lack of systematic cohesiveness in a "body" of knowledge organized in ramified articulation with a single (or dual) dependence on ultimate "beginning(s)", on ἀρχή (or ἀρχαί): This is how the point is being put in the relevant Menonian passage: true beliefs do not last for long in the mind, but tend to flee in time away from it, and so are not of great value, ὅστε οὐ πολλοῦ ἄξιαί εἰσιν, ἕως ἄν τις αὐτὰς δήση αἰτίας λογισμῷ. τοῦτο δ' ἐστίν, ὧ Μένων ἑταῖρε, ἀνάμνησις, ὡς ἐν τοῖς πρόσθεν ἡμῖν ὡμολόγηται. ἐπειδὰν δὲ δεθῶσιν, πρῶτον μὲν ἐπιστῆμαι

γίγνονται, ἔπειτα μόνιμοι καὶ διὰ ταῦτα δὴ τιμιώτερον ἐπιστήμη ὀρθῆς δόξης ἐστίν, καὶ διαφέρει δεσμῷ ἐπιστήμη ὀρθῆς δόξης (98a3-8). True beliefs become permanent scientific acquisitions of mind by being "bound" to it. And this fixation is being effected by adducing the λογισμὸς αἰτίας, the thought-connection to the *cause*, the calculus which starts with *principles*. Now the transformation of true belief into knowledge has been affirmed before (ἐν τῆς πρόσθεν ἡμῖν ωμολόγηται) to be the work of ἀνάμνησις (as essential learning). "Before" refers to 86a7-8: ...ἐνέσονται αὐτῷ (sc. to man) ἀληθεῖς δόξαι, α \hat{i} έρωτήσει έπεγερθεῖσαι έπιστῆμαι γίγνονται. The awakening of what is lumbering in the soul, the arousing of what is latent, by means of dialectical questioning, constitutes precisely the process of ἀνάμνησις. Now at the end of the dlialogue this is identified with λόγον διδόναι and indeed λόγον τῆς αἰτίας. It is a step forward: to the doctrine of the kinship of nature, and its conjugate tenet on the cohesion of knowledge, it is here summarily but explicitly added that kinship and cohesion, the systematic connectedness of reality and truth, is due to the fact that being and intelligibility proceed from principles (causes), and, ultimately, from ultimate principles (causes). Altí α is left (deliberately) generally meant in the *Meno*: it can refer to the (mediate) causality of the ideas, according to the classical Theory of Ideas as in the Phaedo; it can also refer to the final causality of the Idea of Goodness as in the Republic; it can further refer, to the category of (efficient) causality as in the *Philebus* and the *Timaeus*; and it can finally refer equally well to the ultimate causality of the Principles of Being as in the Unwritten Doctrines, the $\pi \epsilon \varphi i$ τὰγαθοῦ seminar and the Aristotelian testimony. By introducing, as if accidentally, this notion of αὶτία at the end of the dialogue, Plato points to the reason of being's cohesiveness and, *ipso facto*, to the reason of the possibility of scientific knowledge: this reason consisting in being's (and thereby truth's) dependence on – or analysis in – first principles. Given the Pythagoreanism of the setting, these principles have to be the principles of number, π έρας and ἄ π ειρον. On this reading, we have already here presupposed the doctrine of the mathematical structure of reality, of the mathematical constitution of being.

It is so very alluring, on closer analysis, to discover intriguing traces, dispersed providentially by Plato, the creator of his own work-world, all over the corpus, of a complete "system", whose differing aspects and parts are expressed in the various dialogues according to a magisterial plan, a feat of calculativeness.

III

The Platonic dialogues appear to be pieces of a gigantic teaching programme. They provide examples of what they profess to illustrate, dialetical (philosophical) elenchus. Their interpretation is greatly facilitated, if we will take Plato on his word: he handles problems in the way he says they should be handled.

A Platonic dialogue is an act of teaching as Plato understood it. This explains why he is dissatisfied with the written word (*Phaedrus*, 274c-275c-275d-278b), in favour of the oral, living and ensouled word of him who knows (276a8-9; cf. 276a5-7). Plato is for

the awakening-theory of learning, against the transmission-theory. Knowledge involves the principle of its (theoretical and practical) self-validation in all conceivable connections and circumstances; it is not something that can be put in a code and fully expressed by a mechanical rule incapable of "growing" responses in accordance with the encountered situation.

Learning consisting in recollection, the teacher should simply help methodically in the arousing of truth in the learner's mind. This method and process of awaking (on the higher level of truth in the realm of scientific (= philosophical) knowledge) is dialectics. The Platonic dialogue endeavours to reproduce the dynamic life of an oral questioning, guided by the knowledge of the teacher but attentive to the sensibilities of the learner: hence its employment of (philosophical) symbolism, of (philosophical) rhetoric, of (philosophical) artistry, of (philosophical) disputativeness, (philosophical) love, each and all of them according to the needs and merits of the case.

A Platonic dialogue may restrict itself chiefly to the *negative* results of elenchus (the early, "Socratic" dialogues) concentrate on the *road* to genuine knowledge out of the state of $\alpha \pi o \phi (\alpha)$ resulting upon the application of negative dialectics (the "middle" dialogues), or develop themes of *positive dialectics* (always on the lesser side of ultimate sufficiency, even in the latest works). Such an understanding provides the rationale for the traditional division of the Platonic corpus, without in the least invalidating the

fundamental classification according to the existence, and the degree of elaboration, of Pythagoreanism in a Platonic work.

In the Meno the awakening worked up has first of all to do with awakening itself. We have the first written-word exposure of the doctrine of ἀνάμνησις. As to the proclaimed subject of the dialogue (virtue and its teachability), important steps have been taken in its proper understanding. First, excellence (virtue) is intrinsically connected with the truth of things. Second, excellence (virtue) appears to exist as moral and civic virtue unconnected to proper scientific knowledge of reality, and hence unteachable. Third, in such an empirically observable condition, excellence (virtue) can only involve true belief ($\dot{o}\varrho\theta\dot{\eta}$ $\delta\dot{o}\xi\alpha$) and be a matter of, in effect, divine grace. Fourth, applying the recollectin-procedure to that common excellene (virtue), we can transform its associated pattern beliefs into real scientific knowledge. Fifth, of transformation can only be ellected by going thoroughly and deeply into the essential nature of excellence (virtue). (Which means forming a coherent system dependent on first principles, in which excellence (virtue) possesses its natural position).

So, clearly at the end of the dialogue: ἐκ μὲν τοίνυν τούτου τοῦ λογισμοῦ, ὧ Μένων θεία μοίρα ἡμῖν φαίνεται παραγιγνομένη ἡ ἀρετὴ οἶς ἂν παραγίγνηται: τὸ δὲ σαφὲς περὶ αὐτοῦ εἰσόμεθα τότε, ὅταν πρὶν ὧτιη τρόποω τοῖς ἀνθρώποις παραγίγνεται ἀρετή, πρότερον ἐπιχειρήσωμεν αὐτὸ καθ' αὑτὸ ζητεῖν τί ποτ' ἔστιν ἀρετή. νῦν δ' ἐμοὶ μὲν ὥρα ποι ἰέντι etc. (100b2-7). The presumably promised enterprise to define excellence (virtue) is carried out in the *Republic*.

I have furthermore suggested above the preliminary character of the *Meno*, vis-à-vis the *Phaedo*, not least with regard to the development of the theory of ἀνάμνησις. Thus we discover a learning Platonic triad: Meno-Phaedo-Republic.